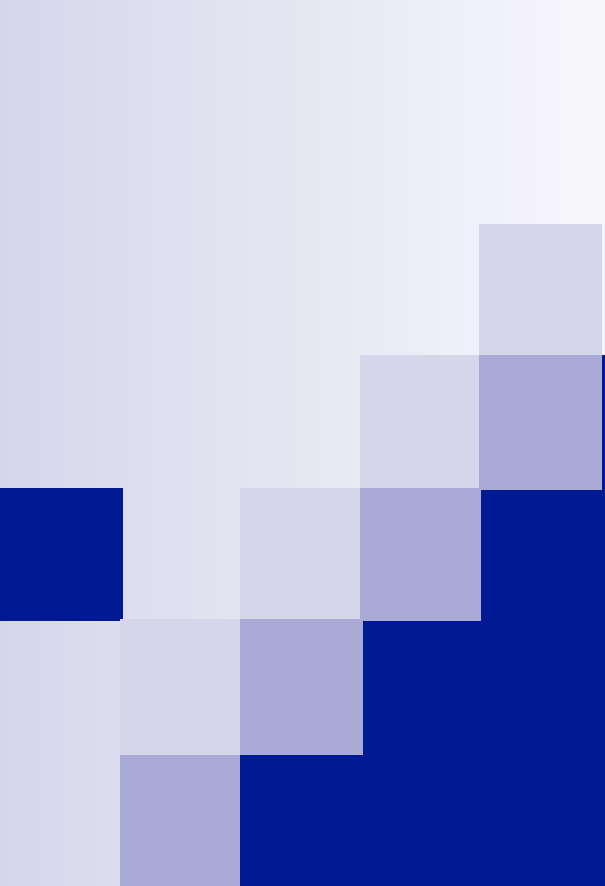




Numerical Overflow (Practice)

ICS312
**Machine-Level and
Systems Programming**

Henri Casanova (henric@hawaii.edu)

(q1) Unsigned Overflow

- For each UNSIGNED operation below say whether it overflows
- 1-byte: $05 + F1$
- 1-byte: $FA + 60$
- 1-byte: $56 - 3F$
- 1-byte: $B3 - FF$
- 2-byte: $FFFF - E410$
- 4-byte: $F6420BA4 + 0A121212$

(q1) Solutions

- For each UNSIGNED operation below say whether it overflows
- 1-byte: $05 + F1$ NO OVERFLOW
- 1-byte: $FA + 60$ OVERFLOW
- 1-byte: $56 - 3F$ NO OVERFLOW
- 1-byte: $B3 - FF$ OVERFLOW
- 2-byte: $FFFF - E410$ NO OVERFLOW
- 4-byte: $F6420BA4 + 0A121212$ OVERFLOW

(q2) Signed Overflow

- For each SIGNED operation below say whether it overflows
- 1-byte: $05 + 7E$
- 1-byte: $FA + 60$
- 1-byte: $76 - 81$
- 1-byte: $B3 - FF$
- 2-byte: $FFFF - E410$
- 4-byte: $F6420BA4 + 7FFFFFFF$

(q2) Solutions

- For each SIGNED operation below say whether it overflows
- 1-byte: $05 + 7E$ OVERFLOW
- 1-byte: $FA + 60$ NO OVERFLOW
- 1-byte: $76 - 81$ OVERFLOW
- 1-byte: $B3 - FF$ NO OVERFLOW
- 2-byte: $FFFF - E410$ NO OVERFLOW
- 4-byte: $F6420BA4 + 7FFFFFFF$ NO OVERFLOW

(q3) Carry bit / Overflow bit

- For each operation below show CF and OF
- 1-byte: $AF + 70$
- 2-byte: $BF12 + 3FFE$
- 1-byte: $AF + 84$
- 2-byte: $5001 + 6FFE$

(q3) Solutions

■ For each operation below show CF and OF

- | | |
|-----------------------|-----------|
| ■ 1-byte: AF + 70 | CF=1 OF=0 |
| ■ 2-byte: BF12 + 3FFE | CF=0 OF=0 |
| ■ 1-byte: AF + 84 | CF=1 OF=1 |
| ■ 2-byte: 5001 + 6FFE | CF=0 OF=1 |

(q4) Carry/Overflow Bit

- For each 1-byte operation below, say whether the overflow bit (of) and the carry bit (cf) configuration is possible (given that one digit can be picked to be any digit between 0 and F)
- $05 + ?E$ $cf=0$ $of=1$
- $14 + ?E$ $cf=1$ $of=1$
- $F2 + 0?$ $cf=1$ $of=0$
- $80 + ?1$ $cf=1$ $of=0$
- $80 + ?1$ $cf=0$ $of=1$
- $A0 + ?4$ $cf=1$ $of=1$

(q4) Solutions

- For each 1-byte operation below, say whether the overflow bit (of) and the carry bit (cf) configuration is possible (given that one digit can be picked to be any digit between 0 and F)

■ $05 + ?E$ $cf=0$ $of=1$

POSSIBLE (e.g., $?=7$)

■ $14 + ?E$ $cf=1$ $of=1$

NOT POSSIBLE

■ $F2 + 0?$ $cf=1$ $of=0$

POSSIBLE (e.g., $?=F$)

■ $80 + ?1$ $cf=1$ $of=0$

NOT POSSIBLE

■ $80 + ?1$ $cf=0$ $of=1$

NOT POSSIBLE

■ $A0 + ?4$ $cf=1$ $of=1$

POSSIBLE (e.g., $?=A$)

(q5) High-Level Code

- Is this way to detect unsigned overflow in some high-level language correct?

```
unsigned int a, b;  
...  
if (a - b < 0) {  
    throw OverflowException;  
}  
unsigned int result = a - b
```

(q5) Solution

- Is this way to detect unsigned overflow in some high-level language correct?

```
unsigned int a, b;
```

```
...
```

NO. Should be “a < b”

```
if (a - b < 0) {
```

```
    throw OverflowException;
```

```
}
```

```
unsigned int result = a - b
```

(q6) High-Level Code

- How should one detect overflow for the following code in some high-level language?

```
unsigned int a, b;  
...  
if ( ??? ) {  
    throw OverflowException;  
}  
unsigned int result = a + b
```

(q6) Solution

- How should one detect overflow for the following code in some high-level language?

```
unsigned int a, b;  
...  
if ( a > UINT_MAX - b ) {  
    throw OverflowException;  
}  
unsigned int result = a + b
```